

# Identity-Based Authenticated Asymmetric Group Key Agreement Protocol

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**Abstract.** In identity-based public-key cryptography, an entity's public key can be easily derived from its identity. The direct derivation of public keys in identity-based public-key cryptography eliminates the need for certificates and solves certain public key management problems in traditional public-key cryptosystems. Recently, the notion of *asymmetric group key agreement* was introduced, in which the group members merely negotiate a common encryption key which is accessible to any entity, but they hold respective secret decryption keys. In this paper, we first propose a security model for identity-based authenticated asymmetric group key agreement (IB-AAGKA) protocols. We then propose an IB-AAGKA protocol which is proven secure under the Bilinear Diffie-Hellman Exponent assumption.

**Keywords:** Identity-Based Public-Key Cryptography, Group Key Agreement, Asymmetric Group Key Agreement, Bilinear Map.

## 1 Introduction

Group Key Agreement (GKA) protocols are widely employed in many modern collaborative and distributed applications. Their main goal is to implement secure broadcast channels. In the conventional GKA definition, a group of members interact over an open network to establish a common secret key to be used to achieve secure broadcast. This secret key is shared by all group members. A limitation of conventional GKA systems is that only group members are allowed to broadcast to other group members. However, in practice, anyone is likely to be a potential sender, just as anyone can encrypt a message in public-key encryption. Observing this fact, Wu *et al.* [17] introduced the notion of Asymmetric Group Key Agreement (AGKA). By their definition, instead of a common secret key, the group members merely negotiate a common encryption key which is accessible to any entity, but they hold respective secret decryption keys.

**Motivation.** In the real world, sometimes the bandwidth is not critical for GKA protocols but the round efficiency is. One-round key agreement protocols have

several advantages [11,17] over key agreement protocols in two or more rounds. For instance, imagine a group of friends who wish to share their personal documents via the open network. If a two-round key agreement protocol is employed to establish a secure channel, all friends should be online at the same time. However, if this group of friends live in different time zones, it is difficult for them to be online concurrently.

A trivial way to achieve one-round AGKA is for each member in the group to publish a public key and reserve the respective secret key. To send a message to this group, a sender separately encrypts for each member and generates the group ciphertext by concatenating all the individual ciphertexts. However, this trivial solution leads to a long ciphertext and forces the sender to store all the public keys of the group members. Instead of this solution, Wu *et al.* [17] proposed a one-round AGKA protocol from *scratch*, which means that the protocol participants do not hold any secret values prior to the execution of the protocol.

Though the protocols from scratch are efficient, they are only secure against passive adversaries who just eavesdrop the communication channel. Active adversaries are more powerful since they are assumed to have a complete control of the communication channel. They have the ability to relay, delay, modify, interleave or delete the message flows during the execution of the protocol. In particular, an active adversary is able to mount well-known man-in-the-middle attacks. Hence, it is vital for an AGKA protocol to withstand the attacks from active adversaries. This calls for authenticated key agreement protocols.

An authenticated key agreement protocol is a key agreement protocol which aims to ensure that no entities aside from the intended ones can possibly compute the session key agreed. Authenticated key agreement protocols may be designed under different public-key cryptosystems. A number of key agreement protocols have been proposed under the traditional PKI-based public-key paradigm. In that paradigm, key agreement protocols rely on the entities obtaining each other's certificates, extracting each other's public keys, checking certificate chains (which may involve many signature verifications) and finally generating a shared session key. Furthermore, the management of public-key certificates requires a large amount of computation, storage, and communication. To eliminate such costs, Identity-Based Public Key Cryptography (IB-PKC) was introduced by Shamir [15] in 1984. The main feature of IB-PKC is that the public key of an entity can be easily derived from its identity, such as its telephone number or email address; the corresponding private key can only be derived by a trusted Private Key Generator (PKG) who owns the *master secret* of the system.

**Contribution.** In this paper, we first specify a security model that an Identity-Based Authenticated Asymmetric Group Key Agreement (IB-AAGKA) protocol should satisfy. Our model allows an adversary to adaptively choose his targets, and it captures the IB version of the (modified) common security requirements (*e.g.*, *secrecy*, *known-key security* and *forward secrecy*), which are usually considered in GKA protocols. These newly defined security requirements are described as follows:

- Secrecy requires that only the legitimate participants (group members) can read the messages encrypted by the negotiated public key.
- Known-key security means that, if an adversary learns the group encryption/decryption keys of other sessions, he cannot compute subsequent group decryption keys.
- Forward secrecy ensures that the disclosure of long-term private keys of group members must not compromise the secrecy of the decryption keys established in earlier protocol runs. Specifically, we say a key agreement protocol offers *perfect forward secrecy* if the long-term private keys of all the group members involved may be compromised without compromising any group decryption key previously established by these group members. We say a key agreement offers *partial forward secrecy* if compromise of the long-term keys of one or more specific group members does not compromise the group decryption keys established by these group members.

We also propose a non-trivial one round IB-AAGKA protocol satisfying our security requirements, which we prove in the random oracle model.

Our protocol is based on a specific identity-based multi-signature scheme which we call identity-based batch multi-signature (IB-B-MS), which may itself be interesting in its own right. Our scheme allows  $x$  signers to sign  $t$  messages in such a way that the length of the batch multi-signature consists only of  $t + 1$  group elements. Furthermore, the batch multi-signature can be separated into  $t$  individual multi-signatures.

**Related Work.** Since Diffie and Hellman published their solution to key agreement [8], much attention has been paid to this primitive. Joux [11] was the first who extended key agreement to three parties. We notice that both the Diffie-Hellman and Joux protocols are one-round key agreement protocols. However, when the protocol participants are more than three, it seems knotty to construct key agreement protocols without additional rounds. Over the years, many attempts have been made at extending the Diffie-Hellman and Joux protocols to  $n$  parties. Among them, the Burmester-Desmedt protocol [5] is one of the best-known. This protocol requires two rounds and is the most efficient existing GKA protocol in round efficiency without constraints on  $n$ .

For a key agreement protocol to be usable in open networks, it should be resistant against active adversaries. However, the basic Diffie-Hellman and Joux protocols as well as the Burmester-Desmedt protocol do not authenticate the communication entities. Hence they are not suited for hostile networks where man-in-the-middle attacks may happen. Several protocols have been proposed to add authentication [7,14]; among those, the GKA protocol in [7] is based on IB-PKC. This protocol refers to Katz and Yung's results [12] for an authenticated version and requires two rounds.

The paradigm of provable security subsumes an abstract formalization that considers the protocol environment and identifies its security goals. Bresson *et al.* [4] were the first to formalize the security model for group key agreement protocols. Later, this model was refined by Bresson *et al.* [2,3] and some variants [12,13] of it appeared. These models are widely accepted in proving the security

of GKA protocols. In this paper, we will borrow some ideas from these models to define the security model for IB-AAGKA protocols.

## 2 Bilinear Maps

Let  $\mathbb{G}_1$  and  $\mathbb{G}_2$  be two multiplicative groups of prime order  $q$ , and  $g$  be a generator of  $\mathbb{G}_1$ . A map  $\hat{e} : \mathbb{G}_1 \times \mathbb{G}_1 \rightarrow \mathbb{G}_2$  is called a bilinear map if it satisfies the following properties: (1) Bilinearity:  $\hat{e}(g^\beta, g^\gamma) = \hat{e}(g, g)^{\beta\gamma}$  for all  $\beta, \gamma \in \mathbb{Z}_q^*$ ; (2) Non-degeneracy: there exists  $u, v \in \mathbb{G}_1$  such that  $\hat{e}(u, v) \neq 1$ ; (3) Computability: there exists an efficient algorithm to compute  $\hat{e}(u, v)$  for any  $u, v \in \mathbb{G}_1$ .

The security of our protocol is based on the hardness of following problems.

**Computational Diffie-Hellman (CDH) Problem:** Given  $g, g^\alpha, g^\beta$  for unknown  $\alpha, \beta \in \mathbb{Z}_q$ , compute  $g^{\alpha\beta}$ .

**$k$ -Bilinear Diffie-Hellman Exponent (BDHE) Problem:** [1] Given  $g, h$ , and  $y_i = g^{\alpha^i}$  in  $\mathbb{G}_1$  for  $i = 1, 2, \dots, k, k + 2, \dots, 2k$  as input, compute  $\hat{e}(g, h)^{\alpha^k}$ .

## 3 Security Model

The first security model for AGKA protocols was presented by Wu *et al.* [17]. We note that the security model in [17] only considers passive attackers. In the sequel, we will extend this model to capture the ability of active attackers and integrate the notion of IB-PKC.

### 3.1 Participants and Notations

Let  $\mathbb{P}$  be a set with polynomial-size of potential protocol participants. Each participant in  $\mathbb{P}$  has an identity and a private key. Any subset  $\mathbb{U} = \{\mathcal{U}_1, \dots, \mathcal{U}_n\} \subseteq \mathbb{P}$  may decide at any point to establish a confidential channel among them. We use  $\Pi_{\mathcal{U}_i}^\pi$  to represent instance  $\pi$  of participant  $\mathcal{U}_i$  involved with partner participants  $\{\mathcal{U}_1, \dots, \mathcal{U}_{i-1}, \mathcal{U}_{i+1}, \dots, \mathcal{U}_n\}$  in a session. Each instance  $\Pi_{\mathcal{U}_i}^\pi$  holds the variables  $\text{pid}_{\mathcal{U}_i}^\pi, \text{sid}_{\mathcal{U}_i}^\pi, \text{ms}_{\mathcal{U}_i}^\pi, \text{ek}_{\mathcal{U}_i}^\pi, \text{dk}_{\mathcal{U}_i}^\pi$  and  $\text{state}_{\mathcal{U}_i}^\pi$  which are defined below:

- $\text{pid}_{\mathcal{U}_i}^\pi$  is the *partner ID* of instance  $\Pi_{\mathcal{U}_i}^\pi$ . It is a set containing the identities of the participants in the group with whom  $\Pi_{\mathcal{U}_i}^\pi$  intends to establish a session key including  $\mathcal{U}_i$  itself. For simplicity, we assume that the identities in  $\text{pid}_{\mathcal{U}_i}^\pi$  are lexicographically ordered.
- $\text{sid}_{\mathcal{U}_i}^\pi$  is the *session ID* of instance  $\Pi_{\mathcal{U}_i}^\pi$ . We follow [13] in assuming that unique session IDs are provided by some higher-level protocol when the group key-exchange protocol is first initiated. Therefore, all members taking part in a given execution of a protocol will have the same session ID.
- $\text{ms}_{\mathcal{U}_i}^\pi$  is the concatenation of all messages sent and received by  $\Pi_{\mathcal{U}_i}^\pi$  during its execution, where the messages are ordered by round, and within each round lexicographically by the identities of the purported senders.
- $\text{ek}_{\mathcal{U}_i}^\pi$  is the encryption key held by  $\Pi_{\mathcal{U}_i}^\pi$ .
- $\text{dk}_{\mathcal{U}_i}^\pi$  is the decryption key held by  $\Pi_{\mathcal{U}_i}^\pi$ .

- $\text{state}_{\mathcal{U}_i}^\pi$  represents the current (internal) state of instance  $\Pi_{\mathcal{U}_i}^\pi$ . When an instance has *terminated*, it is done sending and receiving messages. We say that an IB-AAGKA protocol has been *successfully terminated* (accepted) in the instance  $\Pi_{\mathcal{U}_i}^\pi$  if it possesses  $\text{ek}_{\mathcal{U}_i}^\pi (\neq \text{null})$ ,  $\text{dk}_{\mathcal{U}_i}^\pi (\neq \text{null})$ ,  $\text{pid}_{\mathcal{U}_i}^\pi$  and  $\text{sid}_{\mathcal{U}_i}^\pi$ .

**Definition 1 (Partnering).** We say instances  $\Pi_{\mathcal{U}_i}^\pi$  and  $\Pi_{\mathcal{U}_j}^{\pi'}$  (with  $i \neq j$ ) are *partnered* iff (1) they are *successfully terminated*; (2)  $\text{pid}_{\mathcal{U}_i}^\pi = \text{pid}_{\mathcal{U}_j}^{\pi'}$ ; and (3)  $\text{sid}_{\mathcal{U}_i}^\pi = \text{sid}_{\mathcal{U}_j}^{\pi'}$ .

### 3.2 The Model

In GKA protocols, secrecy is the core security definition. In conventional GKA protocols, secrecy is defined by the indistinguishability of the shared common secret key from a random string in the secret key space. However, in our IB-AAGKA, what is negotiated is only a common public encryption key while the group members' secret decryption keys are different. Observe that both conventional GKAs and our IB-AAGKA have the similar final goal of establishing a confidential broadcast channel among users. Hence, we directly use the confidentiality of the final broadcast channel to define the secrecy of an IB-AAGKA protocol. That is, secrecy is defined by the indistinguishability of a message encrypted under the negotiated public key from a random string in the ciphertext space. Specifically, we use the following game which is run between a challenger  $\mathcal{C}$  and an adversary  $\mathcal{A}$  who has full control of the network communications to define the security of IB-AAGKA protocols. This game comes as follows.

**Initial:** At this stage, the challenger  $\mathcal{C}$  first runs  $\text{Setup}(\ell)$  to generate the system parameters  $\text{params}$  and  $\text{master-secret}$ , then gives the resulting  $\text{params}$  to the adversary  $\mathcal{A}$  while keeping  $\text{master-secret}$  secret.

**Training:**  $\mathcal{C}$  is probed by  $\mathcal{A}$  who can make the following queries:

- $\text{Send}(\Pi_{\mathcal{U}_i}^\pi, \Delta)$ : Send message  $\Delta$  to instance  $\Pi_{\mathcal{U}_i}^\pi$ , and output the reply generated by this instance. If  $\Delta = (\text{sid}, \text{pid})$ , this query prompts  $\mathcal{U}_i$  to initiate the protocol using session ID  $\text{sid}$  and partner ID  $\text{pid}$ . Note that the identity of  $\mathcal{U}_i$  should be in  $\text{pid}$ , and if  $\Delta$  is incorrect the query returns *null*.
- $\text{Corrupt}(\mathcal{U}_i)$ : Output the private key of participant  $\mathcal{U}_i$ . We will use it to model (partial) forward secrecy.
- $\text{Ek.Reveal}(\Pi_{\mathcal{U}_i}^\pi)$ : Output the encryption key  $\text{ek}_{\mathcal{U}_i}^\pi$ .
- $\text{Dk.Reveal}(\Pi_{\mathcal{U}_i}^\pi)$ : Output the decryption key  $\text{dk}_{\mathcal{U}_i}^\pi$ . We will use it to model *known-key security*.
- $\text{Test}(\Pi_{\mathcal{U}_i}^\pi)$ : At some point,  $\mathcal{A}$  returns two messages  $(m_0, m_1)$  ( $|m_0| = |m_1|$ ) and an instance  $\Pi_{\mathcal{U}_i}^\pi$ . It is required that  $\Pi_{\mathcal{U}_i}^\pi$  be fresh (see Definition 2).  $\mathcal{C}$  chooses a bit  $b \in \{0, 1\}$  uniformly at random, encrypts  $m_b$  under  $\text{ek}_{\mathcal{U}_i}^\pi$  to produce the ciphertext  $c$ , and returns  $c$  to  $\mathcal{A}$ . Notice that  $\mathcal{A}$  can submit this query only once, and we will use this query to model *secrecy*.

**Response:**  $\mathcal{A}$  returns a bit  $b'$ . We say that  $\mathcal{A}$  wins if  $b' = b$ .  $\mathcal{A}$ 's advantage is defined to be  $\text{Adv}(\mathcal{A}) = |2 \Pr[b = b'] - 1|$ .

**Definition 2 (Freshness).** *An instance  $\Pi_{\mathcal{U}_i}^\pi$  is fresh if none of the following happens:*

1. *At some point,  $\mathcal{A}$  queried  $\text{Dk.Reveal}(\Pi_{\mathcal{U}_i}^\pi)$  or  $\text{Dk.Reveal}(\Pi_{\mathcal{U}_j}^{\pi'})$ , where  $\Pi_{\mathcal{U}_j}^{\pi'}$  is partnered with  $\Pi_{\mathcal{U}_i}^\pi$ .*
2. *A query  $\text{Corrupt}(\mathcal{U}_i)$  was asked before a query of the form  $\text{Send}(\Pi_{\mathcal{U}_i}^\pi, \Delta)$ .*
3. *All the private keys of the participants with  $\text{sid}_{\mathcal{U}_i}^\pi$  are corrupted<sup>1</sup>.*

**Definition 3.** *An IB-AAGKA protocol is said to be secure against semantically indistinguishable chosen-identity and plaintext attacks (Ind-ID-CPA), if no randomized polynomial-time adversary has a non-negligible advantage in the above game. In other words, any randomized polynomial-time Ind-ID-CPA adversary  $\mathcal{A}$  has an advantage  $\text{Adv}(\mathcal{A}) = |2 \Pr[b = b'] - 1|$  that is negligible.*

Here we only consider security against chosen-plaintext attacks (CPA) for our IB-ASGKA protocol. To achieve security against chosen-ciphertext attacks (CCA), there are some generic approaches that convert a CPA secure encryption scheme into a CCA secure one, such as the Fujisaki-Okamoto conversion [9].

## 4 Building Block

We propose the signature scheme which will be used in our IB-AAGKA protocol. Our scheme can be viewed as a special identity-based multi-signature scheme which we call identity-based batch multi-signature (IB-B-MS) scheme. In our scheme, each signer will use a single random value to generate  $t$  signatures on  $t$  different messages. This way, the resulting signature (referred to as batch signature) on  $t$  messages of a signer only consists of  $t + 1$  group elements. Furthermore, our scheme allows signatures on the same message from  $x$  signers to be aggregated into an IB-B-MS of  $t + 1$  group elements. We notice that, when  $t = 1$ , our scheme degenerates into the Gentry-Ramzan multi-signature [10].

### 4.1 Definition

An IB-B-MS scheme consists of the following five algorithms:

- **BM.Setup:** This algorithm takes as input a security parameter  $\ell$  to generate a master-secret and a list of system parameters.
- **BM.Extract:** This algorithm takes as input an entity’s identity  $ID_i$ , and the master-secret to produce the entity’s private key.
- **Sign:** On input  $t$  messages, a signer’s identity  $ID_i$  and private key  $s_i$ , this algorithm outputs a batch signature.
- **Aggregate:** On input a collection of  $x$  batch signatures on  $t$  messages from  $x$  signers, this algorithm outputs a batch multi-signature.
- **BM.Verify:** This algorithm is used to check the validity of a batch multi-signature. It outputs “all valid” if the batch multi-signature is valid; otherwise, it outputs an index set, which means that the multi-signatures on the messages with indices in that set are invalid.

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<sup>1</sup> Since we do not allow  $\mathcal{A}$  to corrupt all the participants in the same session, our game captures partial forward secrecy.

### 4.2 The Model

The security of an IB-B-MS scheme is modeled via the following game between a challenger  $\mathcal{C}$  and an adversary  $\mathcal{A}$ .

**Initial:**  $\mathcal{C}$  first runs `BM.Setup` to obtain a master-secret and `params`, then sends `params` to the adversary  $\mathcal{A}$  while keeping the master-secret secret.

**Training:** The adversary  $\mathcal{A}$  can perform a polynomially bounded number of the following types of queries in an adaptive manner.

- **Extract:**  $\mathcal{A}$  can request the private key of an entity with identity  $ID_i$ . In response,  $\mathcal{C}$  outputs the private key of this entity.
- **Sign:**  $\mathcal{A}$  can request an entity's batch signature on  $n$  messages. On receiving such a query,  $\mathcal{C}$  outputs a batch signature on those messages.

**Forgery:**  $\mathcal{A}$  outputs a set of  $x$  entities whose identities form the set  $\mathbb{L}_{ID}^* = \{ID_1^*, \dots, ID_x^*\}$ , a message  $m^*$  and a multi-signature  $\sigma^*$ . We say that  $\mathcal{A}$  wins the above game if the following conditions are satisfied:

1.  $\sigma^*$  is a valid multi-signature on message  $m^*$  under identities  $\{ID_1^*, \dots, ID_x^*\}$ .
2. At least one of the identities in  $\mathbb{L}_{ID}^*$  has never been submitted during the `BM.Extract` queries and  $m^*$  together with that identity is not involved in the `Sign` queries.

**Definition 4.** *An IB-B-MS scheme is existentially unforgeable under adaptively chosen-message attack if and only if the success probability of any polynomially bounded adversary in the above game is negligible.*

### 4.3 The Scheme

The construction comes as follows.

- **BM.Setup:** On input a security parameter  $\ell$ , the KGC chooses two cyclic multiplicative groups  $\mathbb{G}_1$  and  $\mathbb{G}_2$  with prime order  $q$ , where  $\mathbb{G}_1$  is generated by  $g$  and there exists a bilinear map  $\hat{e} : \mathbb{G}_1 \times \mathbb{G}_1 \rightarrow \mathbb{G}_2$ . The KGC also chooses a random  $\kappa \in \mathbb{Z}_q^*$  as the master-secret and sets  $g_1 = g^\kappa$ , and chooses cryptographic hash functions  $H_1, H_2 : \{0, 1\}^* \rightarrow \mathbb{G}_1$ . The system parameter list is `params` =  $(\mathbb{G}_1, \mathbb{G}_2, \hat{e}, g, g_1, H_1, H_2)$ .
- **BM.Extract:** This algorithm takes as input  $\kappa$  and an entity's identity  $ID_i$ . It generates the private key  $s_i = id_i^\kappa$  for the entity, where  $id_i = H_1(ID_i)$ .
- **Sign:** To sign  $t$  messages  $m_1, \dots, m_t$ , a signer with identity  $ID_i$  and private key  $s_i$  performs the following steps:
  1. Choose a random  $\eta_i \in \mathbb{Z}_q^*$  and compute  $r_i = g^{\eta_i}$ .
  2. For  $1 \leq j \leq t$ , compute  $f_j = H_2(m_j)$ ,  $z_{i,j} = s_i f_j^{\eta_i}$ .
  3. Output the batch signature  $\sigma_i = (r_i, z_{i,1}, \dots, z_{i,t})$ .
- **Aggregate:** Anyone can aggregate a collection of signatures  $\{\sigma_i = (r_i, z_{i,1}, \dots, z_{i,t})\}_{1 \leq i \leq x}$  on the messages  $\{m_j\}_{1 \leq j \leq t}$  from  $x$  signers into a batch multi-signature. In particular,  $\{\sigma_i = (r_i, z_{i,1}, \dots, z_{i,t})\}_{1 \leq i \leq x}$  can be aggregated into  $(w, d_1, \dots, d_t)$ , where  $w = \prod_{i=1}^x r_i$ ,  $d_j = \prod_{i=1}^x z_{i,j}$ .

- **BM.Verify:** To check the validity of the above batch multi-signature  $(w, d_1, \dots, d_t)$ , the verifier computes  $Q = \hat{e}(\prod_{i=1}^s H_1(ID_i), g_1)$  and for  $1 \leq j \leq t$  checks  $\hat{e}(d_j, g) \stackrel{?}{=} \hat{e}(f_j, w) \cdot Q$ . If all the equations hold, the verifier outputs “all valid”; otherwise, it outputs an index set  $\mathbb{I}$ , which means the multi-signatures with indices in that set are invalid.

In the full version [18], we prove the following theorem.

**Theorem 1.** *Suppose an adversary  $\mathcal{A}$  who asks at most  $q_{H_1}$  times  $H_1$  queries,  $q_{H_2}$  times  $H_2$  queries,  $q_e$  times **Extract** queries,  $q_s$  times **Sign** queries with maximal message size  $N$ , and wins the game in Section 4.2 with advantage  $\text{Adv}(\mathcal{A})$  in time  $\tau$ . Then there exists an algorithm to solve the CDH problem with advantage  $\frac{4}{(q_e + q_s + x + 1)^2 e^2} \text{Adv}(\mathcal{A})$  in time  $\tau + \mathcal{O}(2q_{H_1} + q_{H_2} + 4Nq_s)\tau_{G_1}$ .*

### 5 The IB-AAGKA Protocol

In this section, we propose our IB-AAGKA protocol. In the sequel, we will consider a group of  $n$  participants who wish to establish a broadcast channel.

- **Setup:** The same as **BM.Setup**, except that an identity-based signature scheme and a cryptographic hash function  $H_3 : \mathbb{G}_2 \rightarrow \{0, 1\}^\varsigma$  are chosen, where  $\varsigma$  is the bit-length of plaintexts.
- **Extract:** The same as **BM.Extract**.
- **Agreement:** A protocol participant  $\mathcal{U}_i$ , whose identity is  $ID_i$  and private key is  $s_i$ , performs the following steps:
  1. Choose a random  $\eta_i \in \mathbb{Z}_q^*$ , compute  $r_i = g^{\eta_i}$ .
  2. For  $1 \leq j \leq n$ , compute  $f_j = H_2(j)$ ,  $z_{i,j} = s_i f_j^{\eta_i}$ .
  3. Publish  $\sigma_i = (r_i, \varrho_i, \{z_{i,j}\}_{j \in \{1, \dots, n\}, j \neq i})$ , where  $\varrho_i$  is the identity-based signature on  $r_i$ . To keep the whole protocol efficient, one may choose an identity-based signature scheme that supports batch verification [6] to generate  $\varrho_i$ .
- **Enc.Key.Gen:** To get the group encryption key, an entity first checks the  $n$  message-signature pairs  $(r_1, \varrho_1), \dots, (r_n, \varrho_n)$ . If all of these signatures are valid, then the entity computes  $w = \prod_{i=1}^n r_i$ ,  $Q = \hat{e}(\prod_{i=1}^n H_1(ID_i), g_1)$ , and sets the group encryption key as  $(w, Q)$ .
- **Dec.Key.Gen:** Each participant  $\mathcal{U}_i$  checks the  $n$  message-signature pairs  $(r_1, \varrho_1), \dots, (r_n, \varrho_n)$ . If all of these signatures are valid,  $\mathcal{U}_i$  computes  $d_i = \prod_{j=1}^n z_{j,i}$ , and checks  $\hat{e}(d_i, g) \stackrel{?}{=} \hat{e}(f_i, w) \cdot Q$ . If the equation holds,  $\mathcal{U}_i$  accepts  $d_i$  as the group decryption key; otherwise, it aborts.
- **Enc:** For a plaintext  $m$ , an entity generates the ciphertext as follows:
  1. Select  $\rho \in \mathbb{Z}_q^*$ , compute  $c_1 = g^\rho$ ,  $c_2 = w^\rho$ ,  $c_3 = m \oplus H_3(Q^\rho)$ .
  2. Output the ciphertext  $c = (c_1, c_2, c_3)$ .
- **Dec:** To decrypt the ciphertext  $c = (c_1, c_2, c_3)$ ,  $\mathcal{U}_i$ , whose group decryption key is  $d_i$ , computes  $m = c_3 \oplus H_3(\hat{e}(d_i, c_1)\hat{e}(f_i^{-1}, c_2))$ .

In the full version [18], we prove the following theorem.

**Theorem 2.** *Suppose an adversary  $\mathcal{A}$  who asks at most  $q_{H_1}$  times  $H_1$  queries,  $q_{H_2}$  times  $H_2$  queries,  $q_{H_3}$  times  $H_3$  queries,  $q_c$  times **Corrupt** queries,  $q_s$  times **Send** queries,  $q_{er}$  times **Ek.Reveal** queries and  $q_{dr}$  times **Dk.Reveal** queries, and wins the game with advantage  $\text{Adv}(\mathcal{A})$  in time  $\tau$ . Then there exists an algorithm to solve the  $k$ -BDHE problem with advantage  $\frac{4(1-k\text{Adv}_{sig}(\mathcal{A}))}{q_{H_3}(q_c+q_{dr}+k+1)^2e^2}\text{Adv}(\mathcal{A})$  in time  $\tau + \mathcal{O}(q_{er})\tau_{\hat{e}} + \mathcal{O}(2q_{H_1} + q_{H_2} + kq_s)\tau_{G_1}$ , where  $\text{Adv}_{sig}(\mathcal{A})$  is the advantage for  $\mathcal{A}$  to forge a valid identity-based signature in time  $\tau$ ,  $\tau_{\hat{e}}$  is the time to compute a pairing and  $\tau_{G_1}$  is the time to compute a scalar multiplication in  $\mathbb{G}_1$ .*

## 6 Conclusion

We have defined a security model for IB-AAGKA protocols and proposed a one-round IB-AAGKA protocol from bilinear maps based on the  $k$ -BDHE assumption in the random oracle model. The new protocol allows an adversary to adaptively choose his targets, and it offers the key secrecy, known-key security and partial forward secrecy properties. This design is also readily adaptable to implement broadcast encryption in newly emerging vehicular ad hoc networks [16] to provide secure value-added services.

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